

Unit 7B Day 24: Completing the Square to make Vertex form

Focus Question: How do I complete the square?

A. Review

1. Write the square that created each of the following perfect square trinomials.

a. $x^2 + 30x + 225$

$a=1 \text{ or } 1^2$
 $c=225 \text{ or } 15^2$

$(x+15)^2$

b. $x^2 - 14x + 49$

$a=1 \text{ or } 1^2$
 $c=49 \text{ or } (-7)^2$

$(x-7)^2$

c. $4x^2 - 20x + 25$

$a=4 \text{ or } 2^2$
 $c=25 \text{ or } 5^2$

$(2x-5)^2$

2. Fill in each blank to turn each binomial into a perfect square trinomial. Then write the binomial that was squared.

a. $x^2 - 12x + \underline{\hspace{2cm}}$

$(x-6)^2$

$a=1 \text{ or } 1^2$
 $b=-12$
 $\frac{b}{2a} = \frac{-12}{2(1)} = -6$
 $c=36 \text{ or } (-6)^2$

b. $x^2 + 40x + \underline{\hspace{2cm}}$

$(x+20)^2$

$a=1 \text{ or } 1^2$
 $b=40$
 $c=20^2 \text{ or } 400$
 $\frac{40}{2(1)} = 20$

*c. $4x^2 + 48x + \underline{\hspace{2cm}}$

$(2x+12)^2$

$a=4 \text{ or } 2^2$
 $b=48$
 $c=12^2 \text{ or } 144$
 $\frac{48}{2(2)} = 12$

3. If you are adding a value to the expression or equation, what must you remember to do so that you are not changing the value of the function?

$f(x) = ax^2 + bx + c + \frac{\#}{+5} - \frac{\#}{-5}$

B. We now know enough to turn simple standard form quadratics ($a=1$ and b is even) into vertex form by completing the square!

1) $f(x) = x^2 - 28x - 4$

$= x^2 - 28x + 196 - 4 - 196$

$a=1 \text{ or } 1^2$
 $b=-28$
 $\frac{-28}{2(1)} = -14$
 $c=(-14)^2 \text{ or } 196$

2) $g(x) = x^2 + 4x - 23$

$= x^2 + 4x + 4 - 23 - 4$

$a=1 \text{ or } 1^2$
 $b=4$
 $\frac{4}{2(1)} = 2$
 $c=2^2 \text{ or } 4$

$f(x) = (x-14)^2 - 200$
 $g(x) = (x+2)^2 - 27$

3) $h(x) = x^2 - 12x + 16$

$= x^2 - 12x + 36 + 16 - 36$

$h(x) = (x-6)^2 - 20$

4) $j(x) = x^2 + 2x + 16$

$= x^2 + 2x + 1 + 16 - 1$

$j(x) = (x+1)^2 + 15$

$a=1 \text{ or } 1^2$
 $b=-12$
 $c=(-6)^2 \text{ or } 36$

$a=1 \text{ or } 1^2$
 $b=2$
 $c=1^2 \text{ or } 1$

5) $p(x) = x^2 - 6x + 1$

$$x^2 - 6x + 9 + 1 - 9 = (x-3)^2 - 8$$

$a = 1 \text{ or } 1^2$
 $b = -6$
 $\frac{-6}{2(1)} = -3$
 $c = (-3)^2 \text{ or } 9$

6) $m(x) = x^2 - 10x + 45$

$$x^2 - 10x + 25 + 45 - 25 = (x-5)^2 + 20$$

$a = 1 \text{ or } 1^2$
 $b = -10$
 $\frac{-10}{2(1)} = -5$
 $c = (-5)^2 \text{ or } 25$

C. Completing the Square $a \neq 1$ or b is odd

Turn the following standard form quadratics into vertex form.

1) $f(x) = 2x^2 + 8x - 9$

$$= 2x^2 + 8x - 9$$

$$= 2(x^2 + 4x + 4) - 9 - 2(4)$$

$$= 2(x+2)^2 - 9 - 8$$

$$= 2(x+2)^2 - 17$$

$a = 1 \text{ or } 1^2$
 $b = 4$
 $\frac{4}{2(1)} = 2$
 $c = 2^2 \text{ or } 4$

2) $g(x) = x^2 + 7x + 2$

$$x^2 + 7x + \frac{49}{4} + 2 - \frac{49}{4}$$

$$= (x + \frac{7}{2})^2 + \frac{8}{4} - \frac{49}{4}$$

$$= (x + \frac{7}{2})^2 - \frac{41}{4}$$

$a = 1 \text{ or } 1^2$
 $b = 7$
 $\frac{7}{2(1)} = \frac{7}{2}$
 $c = (\frac{7}{2})^2 \text{ or } \frac{49}{4}$

3) $k(x) = -\frac{1}{4}x^2 - 3x + 6$

$$= -\frac{1}{4}x^2 - 3x + 6$$

$$= -\frac{1}{4}(x^2 + 12x + 36) + 6 + \frac{1}{4}(36)$$

$$= -\frac{1}{4}(x+6)^2 + 6 + 9$$

$$= -\frac{1}{4}(x+6)^2 + 15$$

$a = 1 \text{ or } 1^2$
 $b = 12$
 $\frac{12}{2(1)} = 6$
 $c = 6^2 \text{ or } 36$

4) $h(t) = t^2 - 3t + 2$

$$t^2 - 3t + \frac{9}{4} + 2 - \frac{9}{4}$$

$$= (t - \frac{3}{2})^2 + \frac{8}{4} - \frac{9}{4}$$

$$= (t - \frac{3}{2})^2 - \frac{1}{4}$$

$a = 1 \text{ or } 1^2$
 $b = -3$
 $\frac{-3}{2(1)} = -\frac{3}{2}$
 $c = (-\frac{3}{2})^2 \text{ or } \frac{9}{4}$

5) $n(w) = -6w^2 - 36w + 40$

$$= -6w^2 - 36w + 40$$

$$= -6(w^2 + 6w + 9) + 40 + 6(9)$$

$$= -6(w+3)^2 + 40 + 54$$

$$= -6(w+3)^2 + 94$$

$a = 1 \text{ or } 1^2$
 $b = 6$
 $\frac{6}{2(1)} = 3$
 $c = 3^2 \text{ or } 9$

6) $r(x) = x^2 + 3x - 10$

$$x^2 + 3x + \frac{9}{4} - 10 - \frac{9}{4}$$

$$= (x + \frac{3}{2})^2 - \frac{40}{4} - \frac{9}{4}$$

$$= (x + \frac{3}{2})^2 - \frac{49}{4}$$

$a = 1 \text{ or } 1^2$
 $b = 3$
 $\frac{3}{2(1)} = \frac{3}{2}$
 $c = (\frac{3}{2})^2 \text{ or } \frac{9}{4}$