

Name: _____ Date: _____

67 The Discriminant

1. Define Rational number and give an example.

Any # that can be written as a ratio of 2 integers Ex: 5, -7, 3.1, $4\bar{7}$, $\frac{15}{4}$

2. Define irrational number and give an example.

Any # that can NOT be written as a ratio of 2 integers Ex: π , $\sqrt{31}$, $\sqrt[3]{20}$, $\frac{6\pi}{5}$

3. Decide if each of the following is rational, irrational, or imaginary.

a) $\sqrt{-4}$	b) $\sqrt{25}$	c) $\sqrt{68}$	d) $\sqrt{-12}$	e) $\sqrt{32}$
im.	Q	Q'	im	Q'

For the following problems, find the discriminant, then check the appropriate column. (You may do the work on the back or on your own paper. *(next pages)*)

#	Function	Discriminant	2 rational real solutions	2 irrational real solutions	1 repeated real solution	2 complex solutions
4	$f(x) = x^2 + 5x + 4$	9	X			
5	$g(x) = x^2 + 10x + 25$	0			X	
6	$h(d) = d^2 - 3d - 2$	17		X		
7	$v(t) = -3t^2 + 5t - 2$	1	X			
8	$s(t) = -2t^2 + 4t - 3$	-8				X
9	$j(x) = 4x^2 - 12x + 9$	0			X	
10	$v(x) = 2x^2 - 9x + 13$	-23				X
11	$p(m) = 6m^2 - 11m - 21$	625	X			
12	$d(x) = \frac{1}{2}x^2 + 3x + 8$	-7				X
13	$r(t) = -t^2 - 4t$	20		X		

HW #67

discriminant $b^2 - 4ac$

- ④ $a=1$ $5^2 - 4(1)(4)$ $9 > 0$ so real
 $b=5$ $25 - 16$ 9 is a perfect sq. so rational
 $c=4$ 9
- ⑤ $a=1$ $10^2 - 4(1)(25)$ $0 = 0$ so repeated
 $b=10$ $100 - 100$
 $c=25$ 0
- ⑥ $a=1$ $(-3)^2 - 4(1)(-2)$ $17 > 0$ so real
 $b=-3$ $9 + 8$ 17 is not a perfect sq. so irrational
 $c=-2$ 17
- ⑦ $a=-3$ $5^2 - 4(-3)(-2)$ $1 > 0$ so real
 $b=5$ $25 - 24$ 1 is a perfect sq. so rational
 $c=-2$ 1
- ⑧ $a=-2$ $4^2 - 4(-2)(-3)$ $-8 < 0$ so imaginary
 $b=4$ $16 - 24$
 $c=-3$ -8
- ⑨ $a=4$ $(-12)^2 - 4(4)(9)$ $0 = 0$ so repeated
 $b=-12$ $144 - 144$
 $c=9$ 0
- ⑩ $a=2$ $(-9)^2 - 4(2)(13)$ $-23 < 0$ so complex
 $b=-9$ $81 - 104$
 $c=13$ -23

(11) $a = 6$ $(-11)^2 - 4(6)(-21)$ $625 > 0$ so real
 $b = -11$ $121 + 504$ 625 is a prft sq so Rational
 $c = -21$ 625

(12) $a = \frac{1}{2}$ $3^2 - 4(\frac{1}{2})(8)$ $-7 < 0$ so complex
 $b = 3$ $9 - 16$
 $c = 8$ -7

(13) $a = -1$ $(-4)^2 - 4(-1)(0)$ $20 > 0$ so real
 $b = -4$ $16 + 4$ 20 is not a prft sq. so irrational
 $c = 0$ 20