

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

#68

↓ Quad.      ↓ linear

$$\begin{array}{r} -5x^2 - 2x + 5 = -4x \\ +4x \quad \quad \quad +4x \\ \hline -5x^2 + 2x + 5 = 0 \end{array}$$

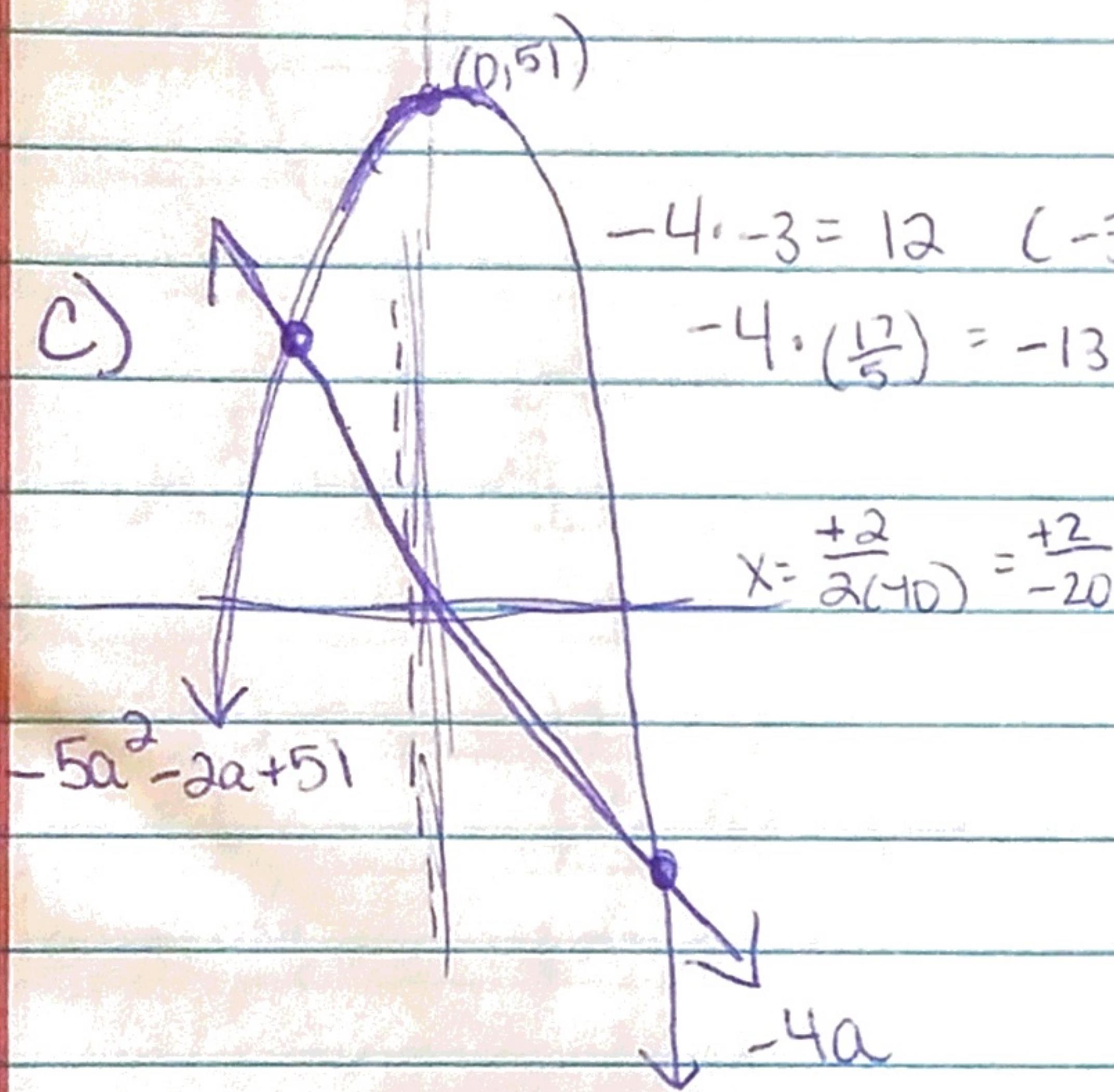
$$\begin{array}{ll} a = -5 & b^2 - 4ac \\ b = 2 & 2^2 - 4(-5)(5) \\ c = 5 & 4 + 1000 \\ & 1024 \end{array}$$

$$x = \frac{-2 \pm \sqrt{1024}}{2(-5)} \Rightarrow \frac{-2 \pm 32}{-10}$$

$$x = \frac{-2 + 32}{-10} \text{ or } x = \frac{-2 - 32}{-10}$$

$$x = \frac{30}{-10} \quad x = \frac{-34}{-10}$$

$$x = \boxed{\frac{17}{5}}$$



b)  $\rightarrow \boxed{x = -3}$

②

↓ Quad.      ↓ zero

$$\begin{array}{ll} 8x^2 + 2x - 15 = 0 & \\ a = 8 & b^2 - 4ac \\ b = 2 & 2^2 - 4(8)(-15) \\ c = -15 & 4 + 480 \\ & 484 \end{array}$$

a) finding x intercepts

$$x = \frac{-2 \pm \sqrt{484}}{2(8)} \Rightarrow \frac{-2 \pm 22}{16}$$

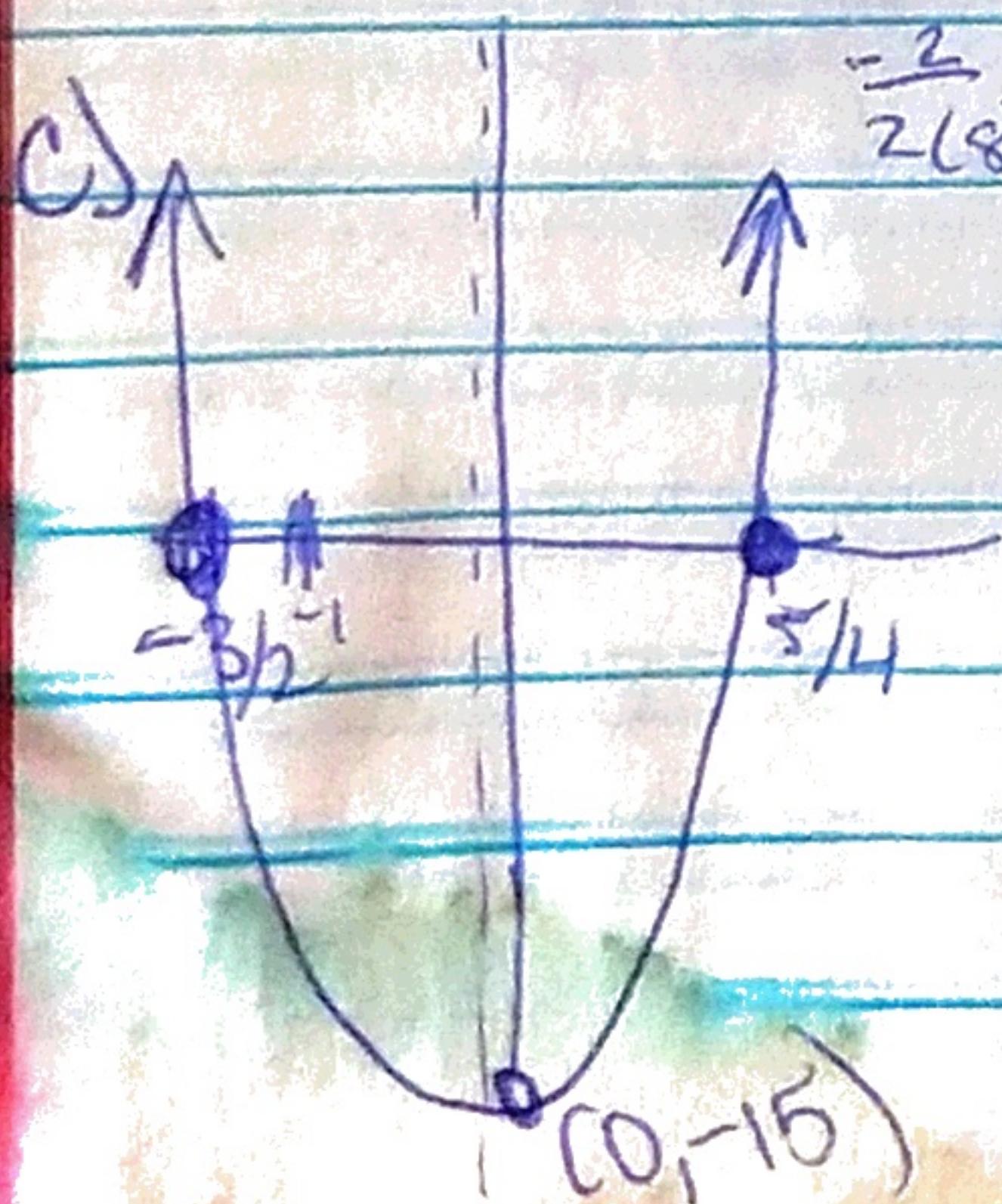
$$x = \frac{-2 + 22}{16} \text{ or } x = \frac{-2 - 22}{16}$$

$$x = \frac{20}{16}$$

$$x = \boxed{-\frac{24}{16}}$$

$$x = \frac{5}{4}$$

$$x = \boxed{-\frac{3}{2}}$$



b)  $\rightarrow \boxed{x = \frac{5}{4}}$

$$\textcircled{3} \quad 5x^2 + 23x + 12 = 0$$

$\nwarrow$  Quad  $\searrow$  zero

$$a = 5$$

$$b = 23$$

$$c = 12$$

$$b^2 - 4ac$$

$$23^2 - 4(5)(12)$$

$$529 - 240$$

$$289$$

a) finding x intercepts

$$x = \frac{-23 \pm \sqrt{289}}{2(5)} \Rightarrow \frac{-23 \pm 17}{10}$$

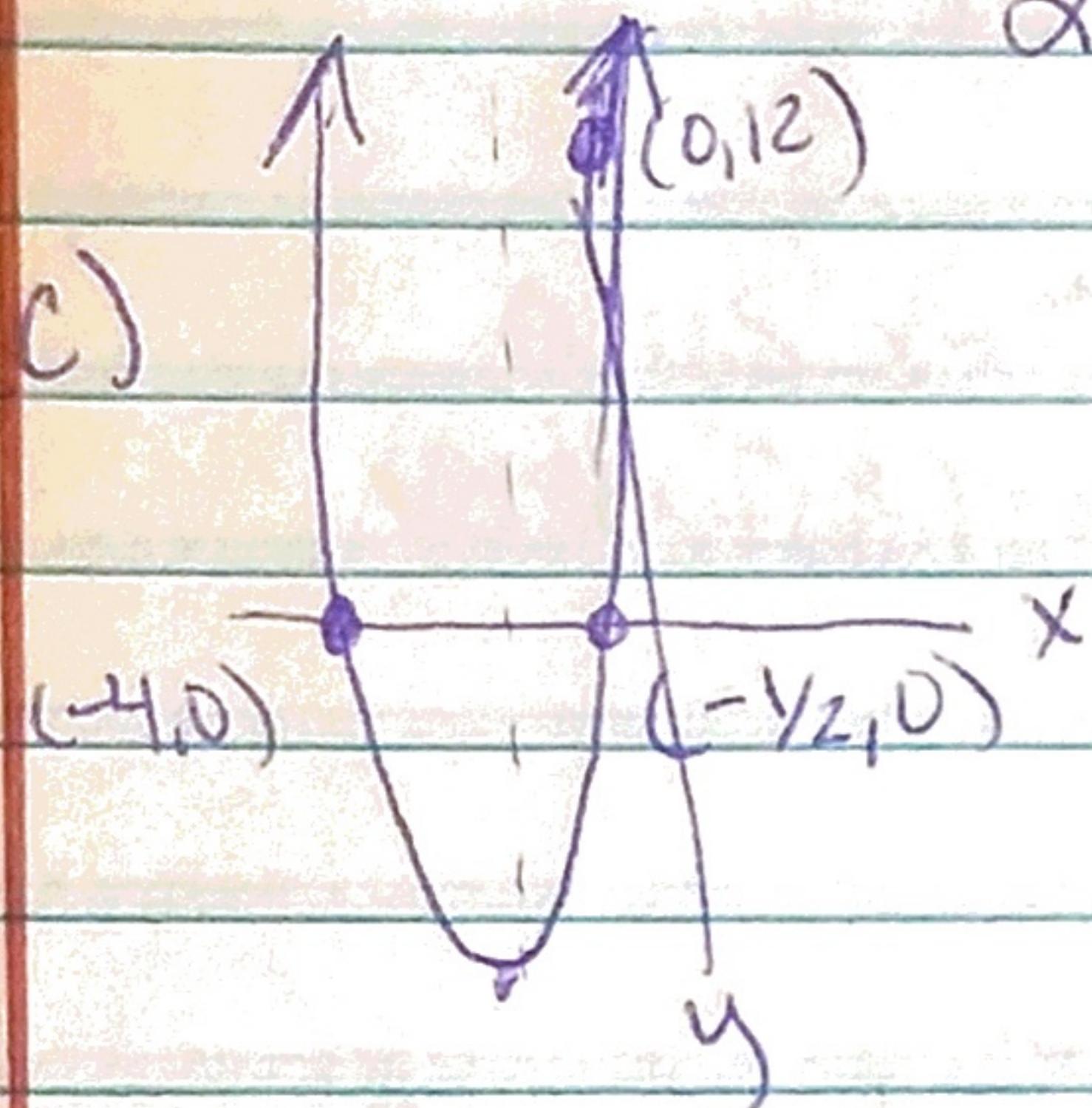
$$x = \frac{-23+17}{10} \text{ or } x = \frac{-23-17}{10}$$

$$x = \frac{-5}{10}$$

$$x = \frac{-40}{10}$$

$$\boxed{x = -\frac{1}{2}}$$

$$\boxed{x = -4}$$



$$\textcircled{4} \quad 10x^2 + x - 9 = 0$$

$\nwarrow$  Quad  $\searrow$  zero

$$a = 10$$

$$b = 1$$

$$c = -9$$

$$b^2 - 4ac$$

$$1^2 - 4(10)(-9)$$

$$1 + 360$$

$$361$$

$$x = \frac{-1 \pm \sqrt{361}}{2(10)} \Rightarrow \frac{-1 \pm 19}{20}$$

$$x = \frac{-1+19}{20} \text{ or } x = \frac{-1-19}{20}$$

$$x = \frac{18}{20}$$

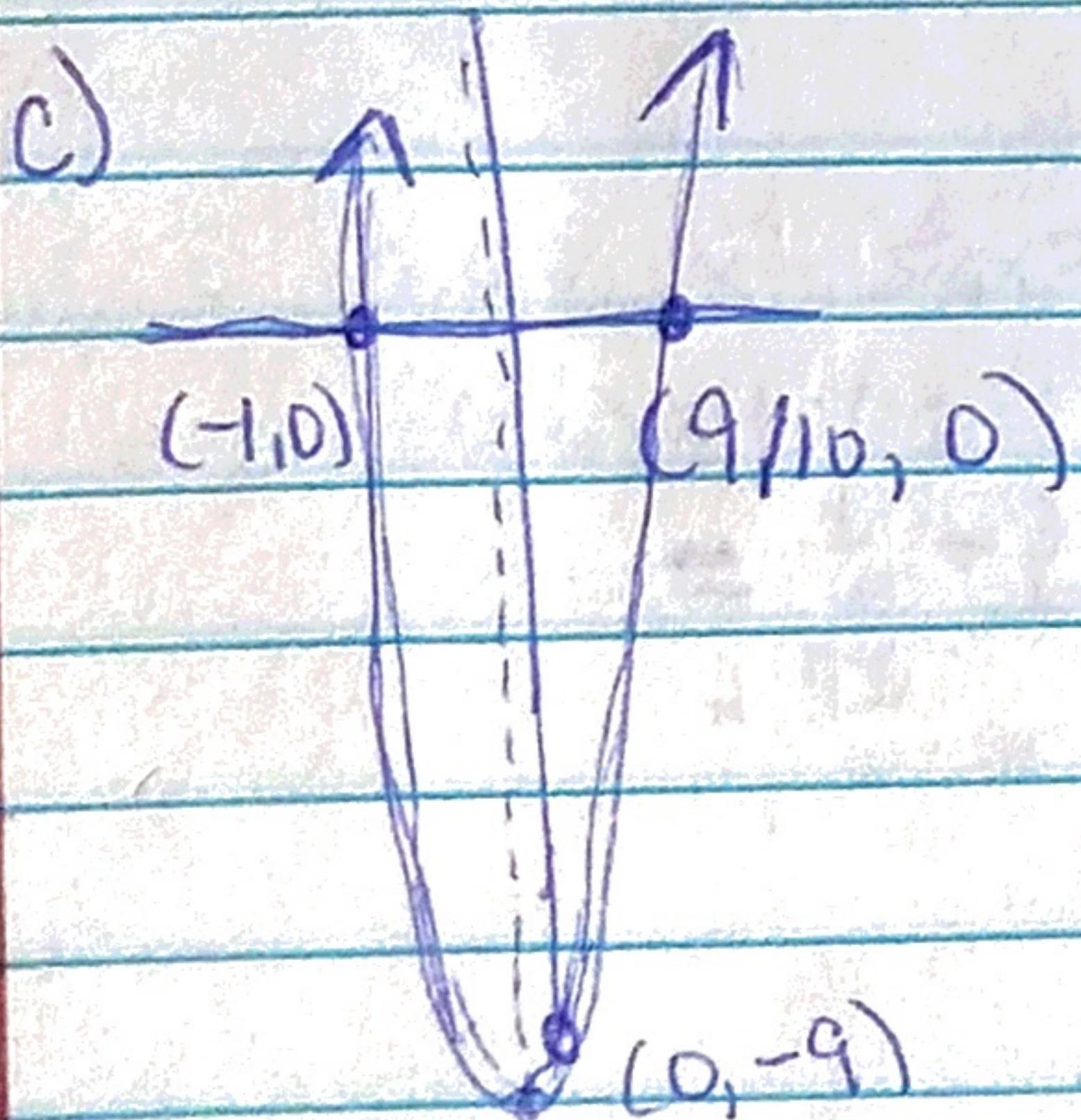
$$\frac{20}{20}$$

$$x = \frac{-20}{20}$$

$$\frac{20}{20}$$

$$\boxed{x = \frac{9}{10}}$$

$$\boxed{x = -1}$$



$$\textcircled{5} \quad 10x^2 - 9x + 6 = 0$$

Quad zero

$$\begin{aligned} a &= 10 & b^2 - 4ac &= (-9)^2 - 4(10)(6) \\ b &= -9 & &= 81 - 240 \\ c &= 6 & &= -159 \end{aligned}$$

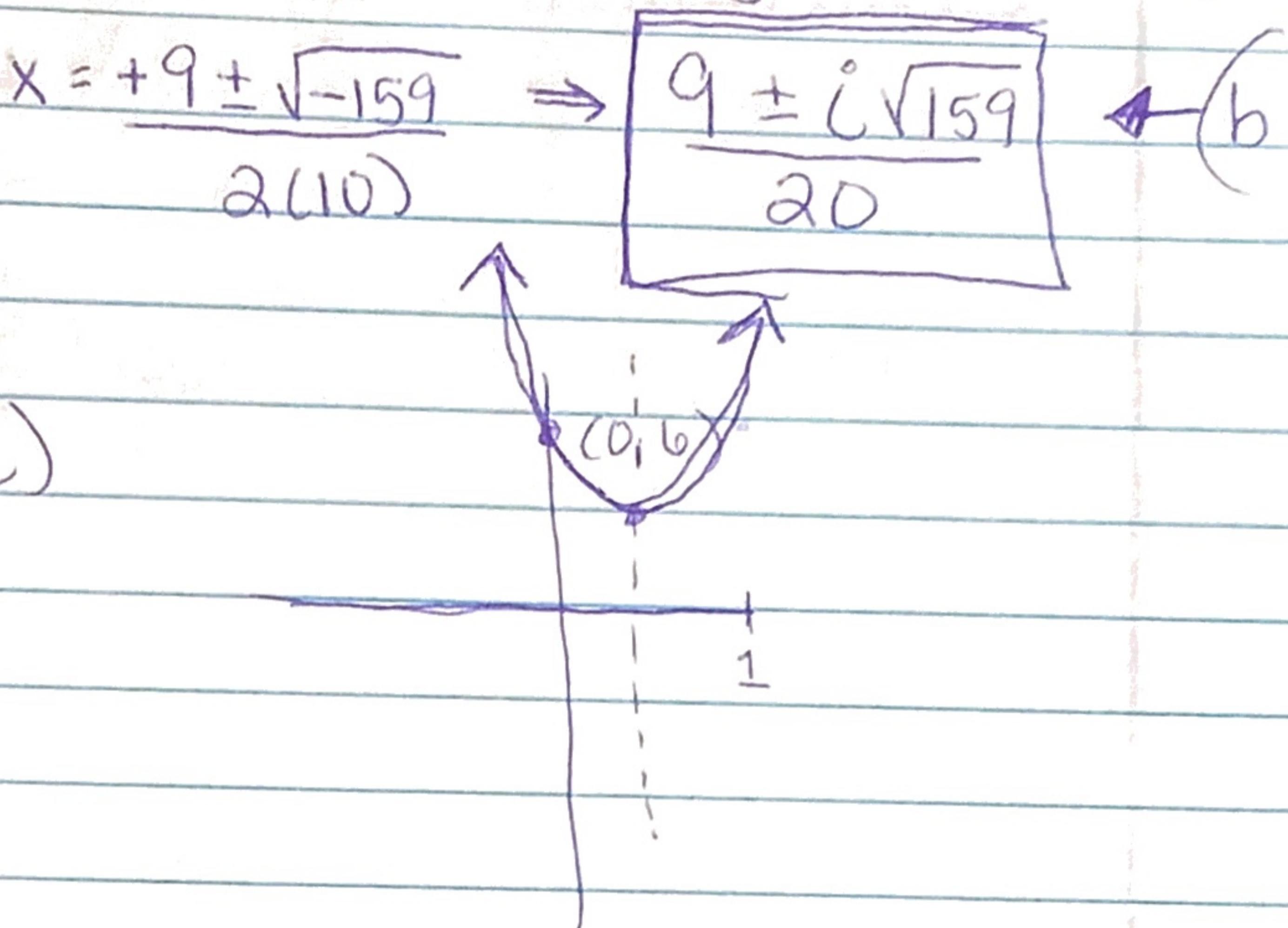
$$\text{a.o.s. } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{9 \pm \sqrt{-159}}{20}$$

$$\text{Vertex if } f\left(\frac{9}{20}\right) = 10\left(\frac{9}{20}\right)^2 - 9\left(\frac{9}{20}\right) + 6$$

$$\approx 2 - 4 + 6$$

$$\approx 4$$

c)



$$\textcircled{6} \quad 6k^2 + 2k + 9 = -3$$

Quad const.

$$\begin{array}{r} +3 \quad +3 \\ \hline 6k^2 + 2k + 12 = 0 \end{array}$$

$$\begin{aligned} a &= 6 & b^2 - 4ac &= 2^2 - 4(6)(12) \\ b &= 2 & &= 4 - 288 \\ c &= 12 & &= -284 \end{aligned}$$

$$x = \frac{-2 \pm \sqrt{-284}}{2(6)} \Rightarrow \frac{-2 \pm \sqrt{4 \cdot -1 \cdot 71}}{12} \Rightarrow \frac{-2 \pm 2i\sqrt{71}}{12}$$

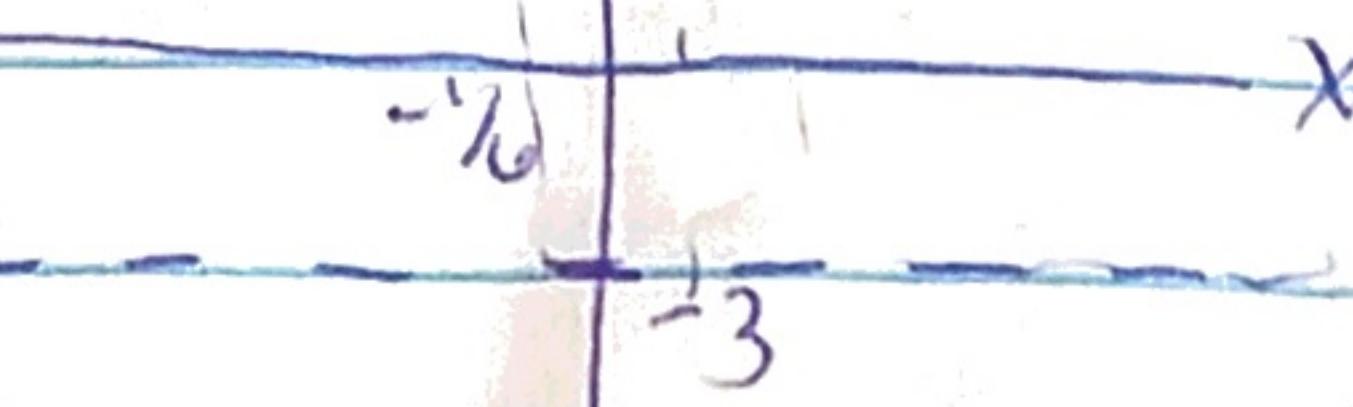
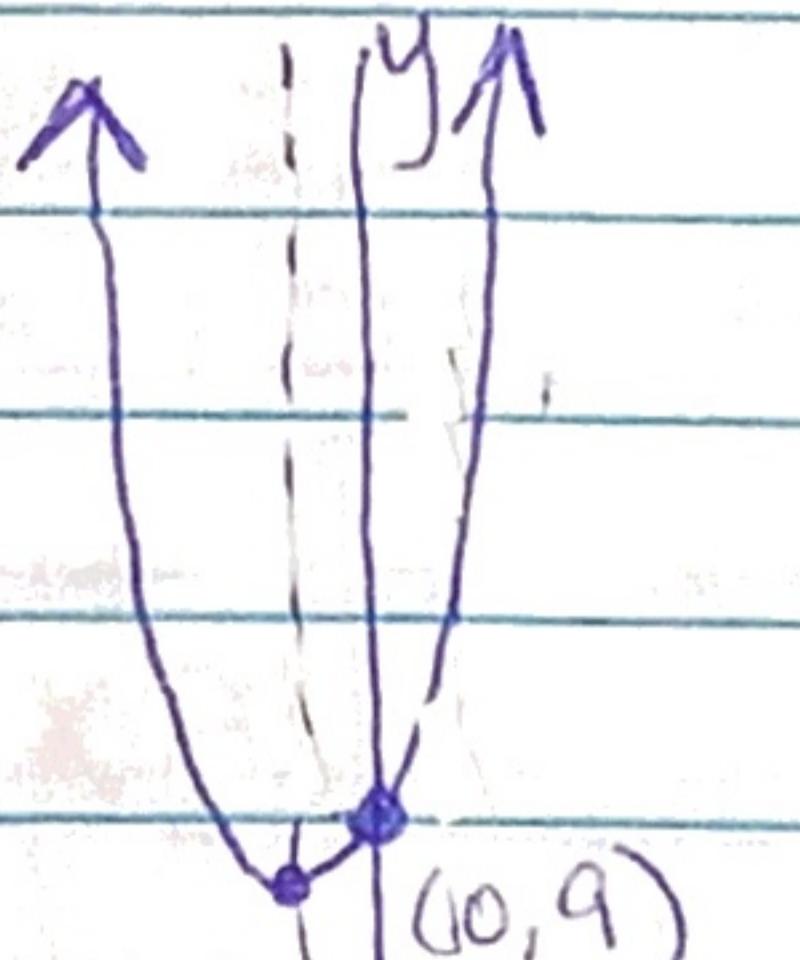
$\frac{2}{12}$  reduces to  $\frac{1}{6}$

$$x = \frac{-1 \pm i\sqrt{71}}{6}$$

$$\text{a.o.s. } x = \frac{-2}{2(6)} = \frac{-2}{12}$$

$$\begin{aligned} f(-\frac{1}{6}) &= 6\left(-\frac{1}{6}\right)^2 + 2\left(\frac{1}{6}\right) + 9 \\ &= \frac{1}{6} + \frac{2}{6} + \frac{54}{6} \\ &= \frac{53}{6} \text{ or } 8\frac{5}{6} \end{aligned}$$

c)

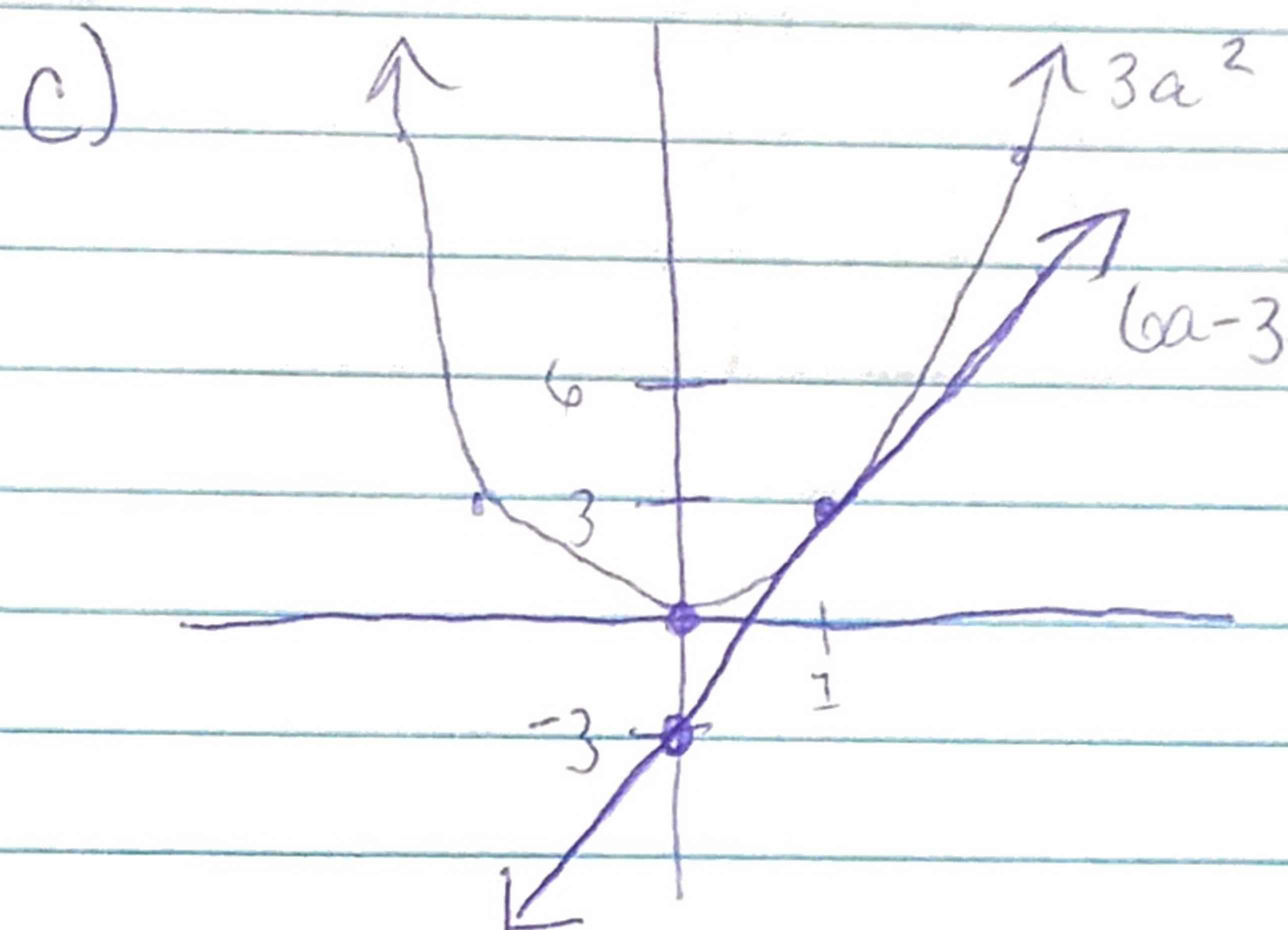


$$\textcircled{7} \quad \begin{array}{c} \text{Quad} \\ 3a^2 = 6a - 3 \\ -(6a + 3) \\ \hline -6a^2 - 6a + 3 \end{array} \quad \begin{array}{c} \text{Linear} \\ 6a - 3 \\ -6a + 3 \\ \hline 0 \end{array}$$

$$3a^2 - 6a + 3 = 0$$

$$\begin{array}{l} a=3 \\ b=-6 \\ c=3 \end{array} \quad \begin{array}{l} b^2 - 4ac \\ (-6)^2 - 4(3)(3) \\ 36 - 36 \end{array}$$

$$x = \frac{-b \pm \sqrt{0}}{2a} \Rightarrow \frac{6 \pm 0}{6} [x = 1] \quad \text{#6}$$



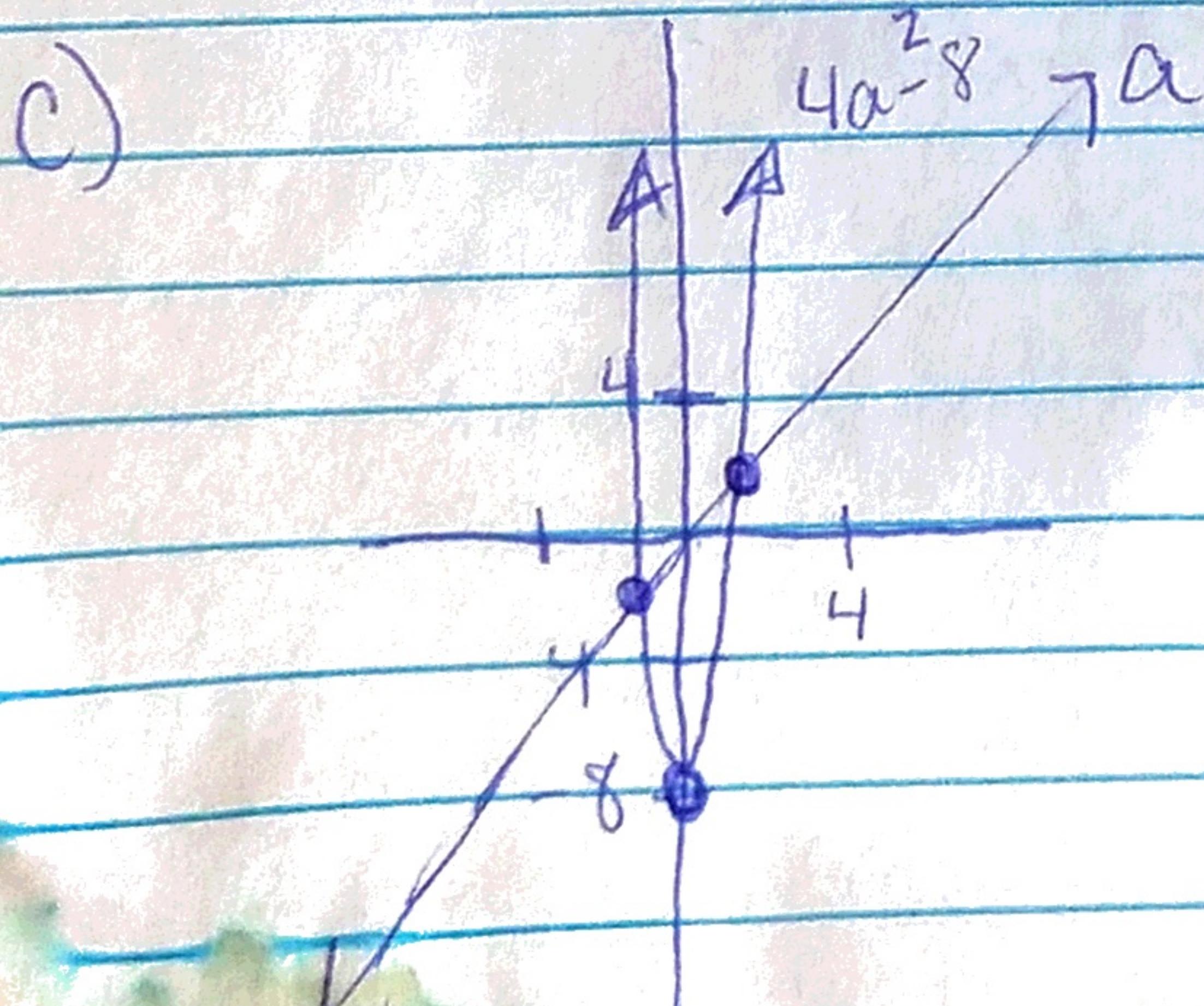
$$\textcircled{8} \quad \begin{array}{c} \text{Quad} \\ 4a^2 - 8 = a \\ -a \quad -a \end{array}$$

$$4a^2 - a - 8 = 0$$

$$\begin{array}{l} a=4 \\ b=-1 \\ c=-8 \end{array} \quad \begin{array}{l} b^2 - 4ac \\ (-1)^2 - 4(4)(-8) \\ 1 + 128 \end{array}$$

$$x = \frac{-1 \pm \sqrt{129}}{2(4)} \Rightarrow \boxed{\frac{-1 \pm \sqrt{129}}{8}} \quad \text{#6}$$

$$x \approx \frac{-1 + 11.36}{8} \quad \text{exact} \quad x \approx \frac{-1 - 11.36}{8}$$



$$\boxed{x \approx 1.3} \quad \boxed{x \approx -1.5}$$