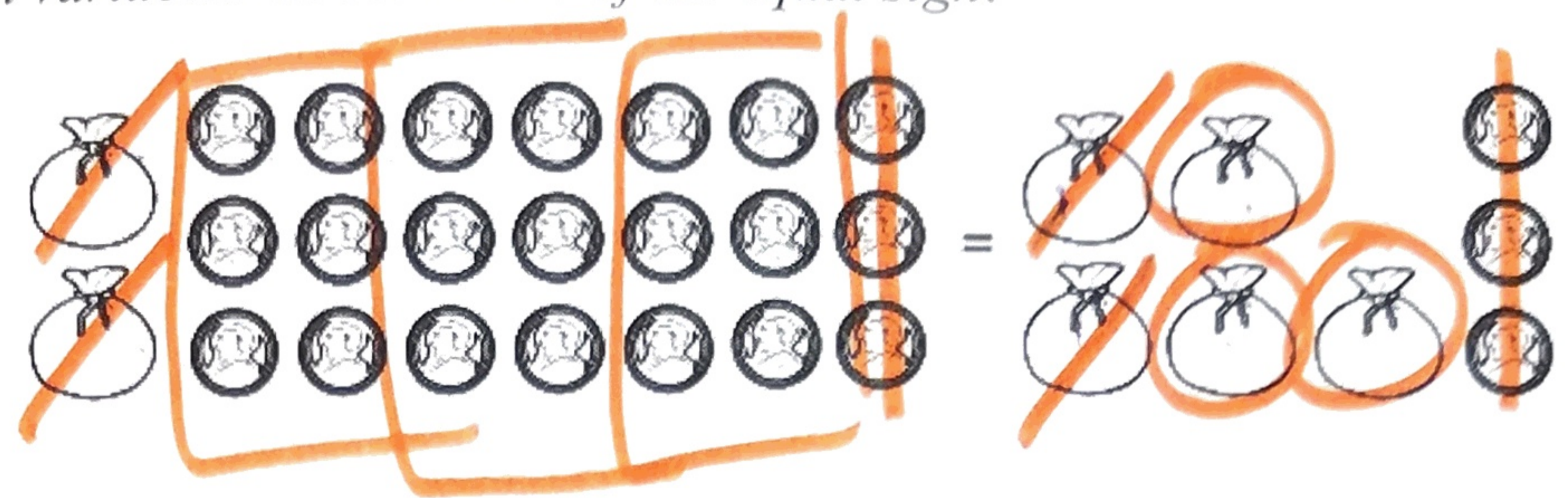


Unit 1 Day 12: Variables on Both Sides

Focus Question: How do I solve an equation with variables on both sides of the equal sign?

A. From a Picture to Symbols

1. How many coins are in each pouch?



2. What does the problem above look like when it is done algebraically?

cis # of coins in a bag

$$\begin{array}{r}
 2c + 21 = 5c + 3 \\
 \underline{-2c} \quad \downarrow \quad \underline{-2c} \\
 21 = 3c + 3 \\
 \underline{-3} \quad \downarrow \quad \underline{-3} \\
 18 = 3c \\
 \underline{\quad} \quad \underline{\quad} \\
 6 = c
 \end{array}$$

An equation is solved when a variable is isolated on one side of the equal sign. In order for this to happen, the variable can only be on one side. **You must decide which side is going to be the variable side before you can continue solving!** You are strongly encouraged to label your choice.

B. Together: Solve each equation below and then check your solution when told.

1. $5n + 12 = 9n - 16$

$$\begin{array}{r}
 5n + 12 = 9n - 16 \\
 \underline{-9n} \quad \downarrow \quad \underline{-9n} \\
 -4n + 12 = -16 \\
 \underline{-12} \quad \underline{-12} \\
 -4n = -28 \\
 \underline{-4} \quad \underline{-4} \\
 n = 7
 \end{array}$$

Check: (substitute)

$$\begin{array}{l}
 5(7) + 12 = 9(7) - 16 \\
 47 = 47 \\
 \text{True so } n=7 \text{ is right}
 \end{array}$$

2. $-7x + 15 = -3 + 2x$

$$\begin{array}{r}
 -7x + 15 = -3 + 2x \\
 \underline{-2x} \quad \downarrow \quad \underline{-2x} \\
 -9x + 15 = -3 \\
 \underline{-15} \quad \underline{-15} \\
 -9x = -18 \\
 \underline{-9} \quad \underline{-9} \\
 x = 2
 \end{array}$$

Check:

$$\begin{array}{l}
 -7(2) + 15 = -3 + 2(2) \\
 1 = 1 \\
 \text{True so } x=2 \text{ is right.}
 \end{array}$$

3. $2(2x + 6) = 2x - 12$

$2 \cdot 2x + 2 \cdot 6$

$4x + 12 = 2x - 12$

$-4x \quad -4x$

$12 = -2x - 12$

$+12 \quad +12$

$24 = -2x$

$-2 \quad -2$

$-12 = x$

4. $-9(c - 4) = 5(c + 20)$

$-9 \cdot c - 9 \cdot -4 = 5 \cdot c + 5 \cdot 20$

$-9c + 36 = 5c + 100$

$+9c \quad +9c$

$36 = 14c + 100$

$-100 \quad -100$

$-64 = 14c$

$14 \div 2 \quad 14$

$-4.571428 = c$

for now

$-\frac{31}{7}$ high school

Practice Rally Coach

A. $5n = 3n - 8$

B. $\frac{x}{4} + 6 = 3x + \frac{1}{2}$

Check:

Chelsea's test had the problem $4(2x - 10) = 6x + 20$. Her work is below. Explain her error(s) in reasoning.

$$\begin{aligned}
 4(2x - 10) &= 6x + 20 \\
 4(2x) + 4(-10) &= 6x + 20 \quad \checkmark \\
 8x - 40 &= 6x + 20 \quad \checkmark \\
 +6x \quad -6x & \\
 14x - 40 &= 20 \\
 +40 \quad +40 & \\
 14x &= 60 \\
 \frac{14x}{14} &= \frac{60}{14} \\
 x &= \frac{30}{7}
 \end{aligned}$$

Chelsea had to solve $4(2x - 10) = 6x + 20$. Her answer was $x = \frac{30}{7}$. But she is wrong b/c she didn't do the same operation on both sides.

At $8x - 40 = 6x + 20$ she should...

$$\begin{aligned}
 8x - 40 &= 6x + 20 \\
 -6x \quad -6x & \\
 2x - 40 &= 20 \\
 \downarrow +40 \quad +40 & \\
 2x &= 60 \\
 \frac{2x}{2} &= \frac{60}{2}
 \end{aligned}$$

$x = 30$